Architecture Personalization in Resource-constrained Federated Learning

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Abstract

Federated learning aims to collaboratively train a global model across a set of clients without data sharing among them. In earlier studies, a global model architecture, either predefined by experts or searched automatically, is applied to all the clients. However, this convention is impractical for two reasons: 1) The clients may have heterogeneous resource constraints and only be able to handle models with particular configurations, imposing high requirements on the model's versatility; 2) Data in the real-world federated system are highly non-IID, which means a model architecture optimized for all clients may not achieve optimal performance on personalized data on individual clients. In this work, we address the above two issues by proposing a novel framework that automatically discovers personalized model architectures tailored for clients' specific resource constraints and data, called Architecture Personalization Federated Learning (APFL). APFL first trains a sizable global architecture and slims it adaptively to meet computational budgets on edge devices. Then, APFL offers a communication-efficient federated partial aggregation (FedPA) algorithm to allow mutual learning among clients with diverse local architectures, which largely boosts the overall performance. Extensive empirical evaluations on three federated datasets clearly demonstrate that APFL provides affordable and personalized architectures for individual clients, costing fewer communication bytes and achieving higher accuracy compared with manually defined architectures under the same resource budgets.

1 Introduction

Recently, some research works have been devoted to Federated Neural Architecture Search (Federated NAS) [1–4]. They aim to search neural architectures in the federated setting where data are not independent and identically distributed (non-IID) among multiple clients (such as mobile phones or online systems of different organizations with constrained data access) and cannot be uploaded to the central server due to privacy concern. Federated NAS finds model architectures automatically, saving much time and human effort compared with the hand-design manner. Thus, it is attracting increasing attention.

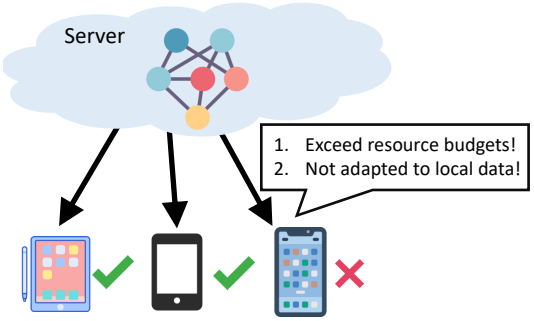

Figure 1: Don't apply the same architecture for all clients.

Existing Federated NAS methods strive to search the optimal *global* model architecture in a decentralized way based on popular NAS algorithms [5–7], which is then applied to all the clients

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after being fully trained. Though effective, two major issues arise when deploying the resultant model architecture on clients. As shown in Figure 1, firstly, each client may have different hardware configurations, posing resource constraints (such as latency, energy and memory footprint) for the architecture to run properly, thus the global architecture maybe not affordable. Secondly, as suggested by [8–10], the architecture that achieves the best performance on particular data distribution may not generalize well to another. In federated learning, the data distributed on clients are non-IID, thus it's implausible that a single architecture optimized globally performs best for all the clients.

To address these issues, this work makes the first effort to explore the problem of discovering personalized architectures that are tailored to specific resource budgets and heterogeneous data distributions of a diverse set of clients in federated learning. This problem is challenging due to privacy and regulatory reasons. Personal data cannot leave the client, thus the architecture search process should take place locally. Most NAS methods are time-consuming and computationally expensive [11, 12]. Though many approaches have accelerated searching or reduce the required computation overhead [5, 13, 14], the inherent drawback of the large search space still remains. So they are not suitable for deployment on resource-constrained edge devices. Further, to boost the local task performance while affording the budget, optimal accuracy-efficiency trade-offs should be achieved.

To battle these problems, we propose a new federated NAS algorithm called *Federated Channel Search (FedCS)*. The main idea is to maintain a powerful global architecture (called "Supernetwork") with strong generalization ability on the server, being tailorable for different clients and then pruning it at the channel-level to obtain efficient and customized local model architectures. Note that local pruning requires no further back-propagation on the local data and can be executed on the fly. Compared with previous federated NAS methods, *FedCS* is more suitable for the resource-constrained federated setting. It largely compresses the scale of search space by only searching for channel configurations. Further, it is computationally-cheap since the searching cost mainly lies in the training process of super-network which could be largely shrunk.

Typically, architectures searched by federated NAS approaches are trained from scratch using FedAvg [15] to boost their performance. However, the parameter aggregation scheme of FedAvg requires each client to share the same architecture and doesn't fit for the setting where each client has diverse architectures. Thus we propose a novel *Federated Partial Aggregation (FedPA)* algorithm to achieve continuous improvements on the performance of sub-networks. In *FedPA*, all the clients collaboratively update the weights of the super-network maintained on the server in a periodic manner, then inherit the corresponding part of weights from the super-network. Since only partial weights of the super-network are transmitted, in our experiments, *FedPA* saves much communication cost to attain the same accuracy with the state-of-the-art FedAvg. Note that *FedPA* is not a supplementary algorithm for *FedCS*, but can be applicable to the general setting where all clients own different architectures sampled from the same search space.

As shown in Figure 2, the primary contribution of this work is a novel *Architecture Personalization Federated Learning (APFL)* framework which includes the above two sequential steps. It addresses a federated learning problem with great practical significance but not much prior literature: each client has its own resource constraint and heterogeneous data and needs to be served with personalized model architecture. *APFL* advances the progress of federated learning in two aspects. 1) First, it provides a computationally-efficient *FedCS* algorithm which conducts neural architecture search for channel number on mobile devices while preserves user privacy. Empirical results show that, with *FedCS*, we are able to acquire personalized architectures which make good trade-offs between accuracy and resource-efficiency. Moreover, personalized architectures searched by *FedCS* cost less communication cost compared with human-designed architectures. 2) Second, *APFL* gives *FedPA*, an off-the-shelf solution to the federated optimization problem under the setting where clients have diverse architectures. Extensive experiments show that *FedPA* achieves much more accuracy gains compared with FedAvg.

2 Related Work

This work is related to Personalization in Federated Learning, Neural Architecture Search, and Federated Neural Architecture Search. Please refer to the Appendix for more discussions.

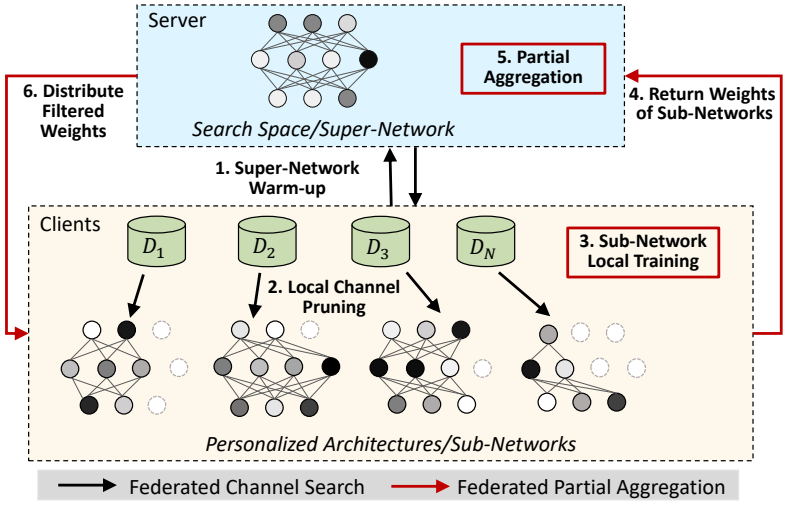

Figure 2: An overview of *APFL* framework. It divides the federated learning process into two subsequent phases: 1) Federated Channel Search (marked with black arrow), which searches hardware-friendly architectures for the clients equipped with heterogeneous resources. 2) Federated Partial Aggregation (marked with red arrow), which aims to make the searched architectures ready for real-time inference.

3 Problem Setup

We consider image classification task on a central server and K clients. Each client u_k stores a local private dataset D^k, with n_k data samples. Each local data sample in D^k is drawn from a local distribution P_k different from the ones of other clients. Their formed global training data $D = \bigcup_k D^k$ with $n = \sum_k n_k$ samples are non-IID.

More specifically, we address a *resource-constrained federated learning* setting. That is, each client u_k has its own computation resource budget B_k. Two resource constraints are considered, *i.e.*, FLOPs and the model size (the number of parameters) which the client can afford.

Formally, we aim to search for the optimal and personalized architecture parameter θ_k^*, along with the optimized model weight parameter w_k^* for each client u_k, whose resource cost $C(\theta_k)$ does not exceed the local budget B_k. The objective can be defined as

$$\begin{aligned} \min_{W,\Theta} \ & F(W,\Theta) \triangleq \sum_{k=1}^{K} p_k \mathcal{L}(w_k, \theta_k; D^k) \\ \text{s.t.} \ & C(\theta_k) \leq B_k, \quad \forall k = 1, 2, ..., K, \end{aligned} \tag{1}$$

$W = [w_1, w_2, ..., w_K]$ denote their corresponding model weight parameters, and $p_k = n_k/n$ is the client-wise weighting factor when participating in aggregation. The function $\mathcal{L}$ is the local objective function which measures the classification loss over the local dataset $D^k = \{z_1, \ldots, z_{n_k}\}$:

$$\mathcal{L}(w_k, \theta_k; D^k) \triangleq \frac{1}{n_k} \sum_{i=1}^{n_k} \ell(w_k, \theta_k; z_i), \tag{2}$$

where $\ell(\cdot, \cdot; \cdot)$ is the cross entropy loss function.

Search Space. Our adopted search space is MobileNet [16–18], which has been proven to be stable and efficient for mobile setting. To further shrink the search space into an acceptable range for resource-constrained federated learning, we set the number of the channels as the only changeable option of the network. Thus, θ is a vector containing the channel configuration of a network. Note that another popular search space DARTS [5] used in [1, 2] is less hardware-friendly and has lower scalability to architecture personalization, thus we don't adopt it.

4 Architecture Personalization Federated Learning (APFL)

Challenges. The above optimization problem is difficult since both the optimal values of W and Θ should be obtained. In this work, we solve it by fixing one and optimizing the other. The problem can be disassembled into two stages: 1) Architecture search, which finds optimal architectures Θ. 2) Personlized Architecture Training, which keeps Θ unchanged and determines the corresponding W. The first sub-question is tricky due to privacy concerns in federated learning. All computation must be completed on resource constrained edge devices, imposing high requirements on the efficiency of the search strategy and the scale of the search space. The second sub-question is also arduous because the heterogeneity of model architectures of clients makes the classic federated optimization algorithm FedAvg fail. More specifically, The underlying assumption of FedAvg is that all clients share the same architecture, while this is not met in our problem.

General Framework. As shown in figure 2, *APFL* consists of two fundamental components: *Federated Channel Search (FedCS)* and *Federated Partial Aggregation (FedPA)*, which are responsible for Architecture Search and Personlized Architecture Training respectively.

FedCS aims to search for the optimal channel configurations which satisfy the resource budgets of individual clients. The general idea is inspired by network pruning [19–22], to reduce a heavy network to a lightweight one by removing redundant weights or neurons. Network pruning is a natural choice for architecture personalization in federated learning, because the same trained super-network can be flexibly applied for local pruning on a large amount of clients. Common pruning criteria includes the magnitudes of weights [23], scaling parameters of batch normalization [19], etc. However, these criteria are not directly applicable to *APFL*. The main reason is that the over-parameterized super-network should be trained in a federated way, thus the numerical values of the weights only reflect the corresponding importance on the global training data D, rather than the importance on the personalized local data D^k. To make the pruned architecture more customized, we propose to ground the pruning criteria on the local task performance. Specifically, we use the instant inference accuracies of the sub-networks contained in the super-network to determine whether a channel should be pruned. Note that we prune at the level of the channel rather than the weight, avoiding unstructured sparse matrix operations which require special hardware support to be effective [17]. To conclude, in *FedCS*, a global tailorable architecture is firstly trained in a distributed way, then it is pruned through client-wise additional learning on the local data to fit the local resource constraints. This approach can fully exploit the generalization properties of the global model as well as the learned customized information from the local distribution.

Algorithm 1: Federated Channel Search. T is the number of communication rounds; E stands for the number of local training epochs; $w_m^{(t)}$ represents the network weights at client u_m in round t; B_k stands for the computation budget at client u_k; C_k is the computation cost of the current network adopted at client u_k, $R \in (0, 1)$ is the shrink ratio of channels.

 # Super-Network Warm-up:
for $t = 0$ *to* $T - 1$ **do**
  Server samples a set of M high capacity clients, indexed by $I^{(t)}$, and broadcasts $w^{(t)}$ to the sampled clients;
  for *each client* u_m *with* $m \in I^{(t)}$ **do**
    $w_m^{(t+1)} \leftarrow \text{TrainingUSNet}(w^{(t)})$
    Send $w_m^{(t+1)}$ back to the server;
  end
  Server aggregates the received gradients as:
  $w^{(t+1)} \leftarrow \sum_{m \in I^{(t)}} \frac{n_m}{n^{(t)}} w_m^{(t+1)}$
end
 # Local Channel Pruning:
Server broadcasts current super-network weights w to all the clients;
for *each client* u_k **do**
  while $C(\theta_k) > B_k$ **do**
    for *number of channels* θ_k^j *for each layer* j **do**
      $\theta_k^j \leftarrow \lceil \theta_k^j (1 - R) \rceil$
      $A^j \leftarrow AccDrop(\theta_k)$
      $\theta_k^j \leftarrow \lfloor \theta_k^j / (1 - R) \rfloor$
    end
    $j^* \leftarrow \arg\min_j A^j$,
    $\theta_k^{j^*} \leftarrow \lceil \theta_k^{j^*} (1 - R) \rceil$
  end
end

FedPA aims to solve the federated optimization problem where the client's architecture are incongruous sub-networks cut out from the super-network. It retains the benefit of collaborative training

by enabling the local customized models to learn from each other. The intuition is to only update the corresponding part of weights in the super-network when a sub-network makes contributions to it.

4.1 Federated Channel Search (FedCS)

FedCS starts with training a sizable global super-network with FedAvg. However, plain training does not optimize the sub-networks contained in the global model. Therefore, the super-network is not a good estimator to rank the relative accuracies of the sub-networks contained in it. So the sub-networks cannot be directly drawn from the super-networks to acquire its instant inference accuracy which will be served as the criteria for local pruning. In view of the above considerations, we resort to slimmable networks [24, 25, 8] which can be executed at arbitrary widths as the global architecture. In slimmable networks, US-Net [25] is particularly suitable because it adopts the sandwich rule and inplace distillation so that sub-networks with different channel configurations can be optimized simultaneously.

Super-Network Warm-up. Different from most network pruning methods, *FedCS* does not fully train the super-network to achieve its utmost performance. The reason is that we only care about the relative accuracy of the sub-networks, so roughly training for 30% of the full rounds will be enough, according to our experiments. This practice benefits federated learning by saving much communication and computation cost. As shown in Algorithm. 1, *FedCS* first initializes the weight of super-network w^0 randomly. In the t-th communication round, the server selects a random subset from the clients which are capable of running the super-network properly, indexed by $I^{(t)} \subseteq \{1, \ldots, K\}$, and distributes the current $w^{(t)}$ to them. Then each participating client u_m performs local training based on the received parameters $w^{(t)}$, and sends the updated parameters $w_m^{(t)}$ back to the central server. Specifically, the typical training paradigm of US-Net is adopted in the local learning procedure, details are covered in the Appendix. After receiving the architecture parameters and network weights from all the participating clients, the central server then takes a weighted average of them to update the global model. The weighting factor is $\frac{n_m}{n^{(t)}}$, where n_m is the number of local samples of the client u_m, and $n^{(t)} = \sum_{m \in I^{(t)}} n_m$ is the total number of data samples used in this communication round.

Local Channel Pruning. Once the super-network is obtained, unnecessary channels are pruned from it layer-wisely. We adopt greedy pruning strategy [8, 26] to achieve an inherent trade-off between the accuracy and the resource-efficiency of the personalized architecture. Local pruning requires no further training of the super-network. The sub-networks can be directly sampled from the super-network to acquire the instant inference accuracy as the pruning criterion. Algorithm. 1 shows the detailed local channel pruning procedure. The central server first broadcasts the weights w of the super-network obtained from the warm-up stage to all clients. After receiving w from the server, each client u_k fine-tunes the channel number of the received architecture based on its local resource budget B_k. Concretely, we predefine a shrink ratio $R \in (0, 1)$. In each iteration, each layer is shrunk by R tentatively, then the accuracy of the pruned network is computed on the local training dataset. After finishing all the layers, the layer j with the minimum accuracy drop A^j will be truly shrunk. Then the computation cost $C(\theta_k)$ of the pruned network will be checked. If it is lower than the local resource budget B_k, the pruning process would be terminated.

4.2 Federated Partial Aggregation (FedPA)

After attaining personalized architectures by *FedCS*, one can choose to fully train them on the local datasets. However, to make the best use of the generalization capacity of the super-network and also the global information encoded in it, the local model can inherit the corresponding part of parameters from the super-network. This is inspired by the lottery ticket hypothesis [27] that sub-networks can benefit from the initial weights of the original super-network. However, as suggested by [28, 29], simply training on the local data restrains individual clients from learning beneficial knowledge from each other and sacrifices the core advantage of federated learning: win-win cooperations among clients. After an extensive survey on federated optimization algorithms, we find that most off-the-shelf methods, such as FedAvg[15], FedMA [30], FedProx [31], are grounded on the assumption that all clients share the same architecture, thus not fit for our problem. In view of this, we propose a novel federated partial aggregation algorithm *FedPA* which solves federated optimization problem with heterogeneous edge architectures. Full details of FedPA can be found in the Appendix.

A crucial trick of FedPA is always to keep batch normalization [32] statistics locally, for three reasons. First, running mean and variance of feature representations are privacy-sensitive, thus should never leave the clients. Second, retaining batch normalization statistics locally is naturally suited to eschew aggregation disorder brought by heterogeneous channel configuration. Additionally, for non-IID data, the local running means and variances may vary across clients considerably, thus average them to accumulate global BN statistics may not help advance local task performance.

5 Experiment

5.1 Experiment Setup

We consider image classification task and adopt three datasets from the popular FedML benchmark [33], including CIFAR-10 [34], CIFAR-100 [34] and CINIC-10 [35]. Note that CINIC-10 is constructed from ImageNet [36] and CIFAR-10, whose samples are very similar but not drawn from identical distributions. Therefore, it naturally introduces distribution shifts which is suited to the heterogeneous nature of federated learning. We are interested in two data partition strategies : IID partition and NIID partition. The detailed partition strategy, statistics and visualizations of the datasets are summarized in the Appendix. For the local resource constraints B_k, we divide the clients into 3 groups with 3 possible resource configurations: high budget, medium budget and low budget. To check the performance of *APFL* under the scenarios with different overall computation capacities, we consider two settings: 1) HIGH CAPACITY, where 50% of clients are equipped with high computation budgets, 30% and 20% of clients have medium and low computation budgets. 2) LOW CAPACITY, where only 20% of clients are equipped with high computation budgets, 30% and 50% of clients have medium and low budgets. Other implementation details are covered in the Appendix.

5.2 Accuracy Improvement of APFL

The classic federated optimization algorithm *FedAvg* requires all clients to share the same architecture. To make it comparable in our setting, we set the global architecture of *FedAvg* as MobileNetV2-0.5x which is acceptable to all the clients. However, this baseline is weak considering the overall computation capacity is still low. So we propose a stronger baseline that allows each client to own heterogeneous local architectures. We term it as *federated learning with uniform channels (FedUniform)*. Concretely, *FedUniform* modifies the global width multiplier of the super-network adaptively for each client till its resource constraints are fulfilled. According to [16, 17], It's effective for trading off between resource efficiency and accuracy. In *FedUniform*, the local architectures adopted by clients with high, medium and, low resource budgets are MobileNetV2 with 1x, 0.75x and, 0.5x width multipliers respectively. The local architectures obtained by *FedCS* and *FedUniform* are both trained with *FedPA* from scratch. Note that for a fair comparison, sub-networks of *FedCS* didn't inherit weights from the super-network which was trained in the warm-up stage. However, we also find that using the parameters of super-networks for initialization further improves the performance of *FedCS*. After training, the local testing tasks can be performed either by downloading the global super-network from the server for inference or directly running with the local architectures. We report accuracies of both evaluation methods and abbreviate them as "Glo" and "Loc".

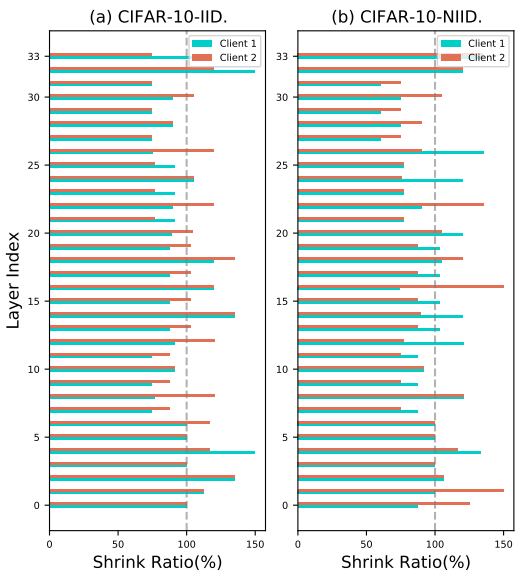

Figure 3: Comparing architectures searched on different clients.

We summarize all the results in Table 1. For all the datasets, it can be observed that *FedCS* achieves accuracy improvements over *FedAvg*, with the accuracy gain up to 15.17% on CINIC-10. We then

Table 1: Accuracy@1 (%) on CIFAR-10, CIFAR-100 and CINIC-10.

	Methods	CIFAR-10				CIFAR-100				CINIC-10			
		IID		NIID		IID		NIID		IID		NIID	
		Glo.	Loc.	Glo.	Loc.	Glo.	Loc.	Glo.	Loc.	Glo.	Loc.	Glo.	Loc.
HIGH CAPACITY	FedAvg	92.10		89.49		66.36		64.6		77.63		60.21	
	FedUniform	92.58	92.55	92.47	92.52	68.1	67.80	65.83	65.46	79.21	79.19	71.11	73.57
	FedCS (Ours)	**92.74**	**92.75**	**93.08**	**93.29**	**68.39**	**68.46**	**66.01**	**65.60**	**79.33**	**79.31**	**74.51**	**75.38**
LOW CAPACITY	FedAvg	92.10		89.49		66.36		64.6		77.63		60.21	
	FedUniform	91.66	91.68	92.38	92.45	67.61	67.51	65.69	65.39	78.76	78.78	71.04	72.22
	FedCS (Ours)	**92.63**	**92.64**	**92.82**	**93.05**	**67.83**	**68.15**	**65.86**	**65.44**	**79.01**	**79.02**	**73.04**	**74.42**

compare *FedCS* with *FedUniform* and find that *FedCS* performs consistently better than *FedUniform*. We also notice that when increasing the proportion of clients with lower resource budgets (from HIGH CAPACITY to LOW CAPACITY), the accuracies of *FedCS* and *FedUniform* both decrease, but *FedCS* still performs better than *FedUniform*. It well demonstrates that the architectures searched by *FedCS* are more customized to the local data distribution. Another surprising discovery is that the performance of applying personalized architectures for local inference is not necessarily worse than that of applying the full super-network. On CINIC-10, it even provides a 2.46% accuracy gain, which further validates the advantage of architecture personalization. To conclude, all results confirm that *FedCS* is able to find personalized architectures which not only meet the local resource constraints but also boost the performance of local tasks.

5.3 Visualization of Personalized Architectures

To analyze the characteristics of the personalized architectures searched by *APFL*, we now provide additional visualization results. First, we compare the local architectures of the clients who belong to the same resource group. On the IID and NIID versions of CIFAR-10, we plot the shrink ratios of the pruned architectures (compared to the original MobileNetV2). As shown in Figure 3, the architectures searched on the NIID version are visually more heterogeneous. We also compute the L2 distance between the two architecture parameters θ and find that the distance between architectures searched on the IID version is indeed smaller. This suggests that the personalized architectures obtained by *APFL* are effectively adapted to local distributions.

5.4 System Overhead

We now present another benefit brought by *FedCS*. As shown in Figure 5, we compare the average FLOPs and number of parameters of local architectures searched by *FedCS* with that of *FedUniform*. It can be seen that with nearly the same FLOPs, *FedCS* provides more lightweight architectures which consume less local storage space than *FedUniform*. As shown Figure 4, training architectures searched by *FedCS* obviously costs fewer communication bytes to achieve the same accuracy as that of *FedUniform*. This is particularly inspiring, as communication cost is the main bottleneck of federated learning.

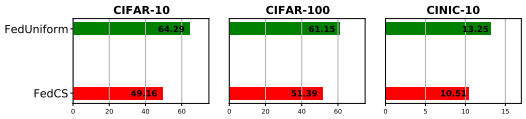

Figure 4: Communication Cost (GBytes).

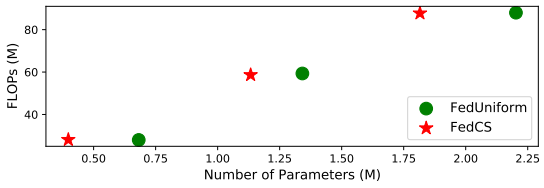

Figure 5: FLOPs and number of parameters.

6 Conclusion

In this paper, we initialize the concept of architecture personalization and propose a novel federated architecture learning framework named *APFL* which is able to discover resource-efficient personalized model architectures for individual clients. Extensive empirical results well demonstrate the effectiveness and high efficiency of *APFL*. As a starting point, we hope the proposed *APFL* framework could contribute to simulating research on architecture personalization in federated learning. We leave to future work many open problems, such as convergence analysis of *FedPA* and more effective federated partial aggregation algorithms.

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A Related Work

Personalization in Federated Learning. Personalization in federated learning aims to make the global model more customized to suit the need of individual users. One line of works incorporate meta-learning and multi-task learning with federated learning [37–41], where a client in federated learning can be directly regarded as a task in meta-learning or multi-task learning. Another line of works learn both global parameters for all clients and local private parameters for individual clients [42, 43]. Different from previous works which aim to personalize model parameters, we focus on personalizing the local architecture for each resource-constrained client in federated learning. To the best of our knowledge, we are the first to study this particular problem.

Neural Architecture Search. Neural Architecture Search (NAS) aims at automating the process of architecture design [11, 44, 45, 5]. Early works on NAS focus on searching for high performance architectures without restricting their computational cost [11, 12, 44, 5], and the resultant architectures may be inefficient for deployment on resource-constrained platforms, such as mobile phones or embedded devices. Recent works [46–50, 8] focus on searching for the architectures that can be deployed on resource-constrained hardware platforms efficiently. They achieve this purpose by incorporating the resource constraints of hardware platforms into the search process or the search space. As a result, the inference efficiency of these searched architecture has been largely improved. However, all these previous NAS methods search the architectures on data which are identically and independently distributed. The NAS algorithms specifically designed for non-IID data await to be studied.

Federated Neural Architecture Search. Several works have been devoted to federated NAS. [1] and [2] develop gradient-based federated NAS algorithms, where each client performs neural architecture search locally, and then synchronizes the variables of the architecture with other workers by weighted aggregation periodically. [3] presents a federated evolutionary NAS algorithm which adopts a sampling strategy for one-shot NAS [51], where only one path of the global model is sampled and sent to the local clients in each communication round. [4] proposes an algorithm based on NetAdapt [7], which iteratively prunes the global model to make it more compact until it meets the resource budgets of all the clients. A major drawback of these previous works is that, they all search for a global architecture which may be non-optimal for some individual clients. By contrast, in our work, we consider searching for client-specific ('personalized') architectures and take resource constraints into consideration, which has never been studied before.

B Local Training of US-Net

Different from training a single neural network whose width is immutable, training an universally slimmable network (US-Net) which can be executed at arbitrary widths at run time is more efficient and flexible. To achieve this goal, two training techniques: sandwich rule and inplace distillation proposed in [25] are adopted. Concretely, these two techniques are applied when updating the global model on the edge clients.

As shown in Algorithm 2, after one client receives the current global model weights $w^{(t)}$ from the server, it will determine the number of sub-networks to extract from the large global model, which is denonted as S. Then the full network with $1\times$ width are first executed on the local dataset and the gradients are accumulated. The stop gradient $y^{(t)}$ is saved as soft label for inplace distillation. Afterwards, the smallest $0.25\times$ network and other $(S-2)$ random sampled networks whose widths are in the range of $(0.25, 1)\times$ are executed sequentially and the corresponding gradients are accumulated. Note that when calculating the loss, the soft label $y^{(t)}$ distilled from the full network is used rather than the ground truth. The essential idea behind this practice is to transfer knowledge from the powerful full network to the sub-networks, thus the convergence may speed up. Finally, the accumulated gradients are applied to update the original model parameters $w^{(t)}$ received from the server, and the updated parameters $w_m^{(t)}$ are returned to the server.

C Federated Partial Aggregation

We present the details of our proposed *Federated Partial Aggregation (FedPA)* in Algorithm 3.

Algorithm 2: TrainingUSNet. S is the number of sub-networks to sample in each local epoch;

Input: $(w^{(t)}, S)$;
for $e = 1$ *to* E **do**
    Sample the networks with largest width $1\times$ and smallest width $0.25\times$, and $(S-2)$ random networks with width between $[0.25, 1]\times$;
    Execute the largest network with width $1\times$, accumulate gradients and stop gradients $y^{(t)}$ as soft labels;
    Execute other $(S-1)$ sub-networks, use $y^{(t)}$ to compute loss and accumulate gradients;
    Update the corresponding parameters in $w^{(t)}$ to form $w_m^{(t)}$ using the accumulated gradients;
end
return $w_m^{(t)}$.

Algorithm 3: Federated Partial Aggregation. $T^{'}$ is the number of the total communication round. $E^{'}$ represents the number of local epochs. z_m is the mask vector of client u_m. γ is the learning rate;

Server initializes w^0 randomly or with pretrained weights from *FedCS*;
for $t = 0$ *to* $T' - 1$ **do**
    Server samples a set of M clients indexed by $I^{(t)}$, checks mask vectors z_m on selected clients u_m and distributes $w^{(t)} \odot z_m$ to them; **for** *each client* u_m *with* $m \in I^{(t)}$ **do**
        for $e = 1$ *to* $E^{'}$ **do**
            $w_m^{(t+1)} \leftarrow w_m^{(t)} - \gamma \nabla \mathcal{L}(w_m^{(t)}; D^m) \odot z_m$;
        end
        return $w_m^{(t+1)}$ to the server;
    end
    server averages the received $w_m^{(t+1)}$ as:
    $w^{(t+1)} \leftarrow \sum_{m \in I^{(t)}} \frac{n_m}{n^{(t)}} w_m^{(t+1)}$
end

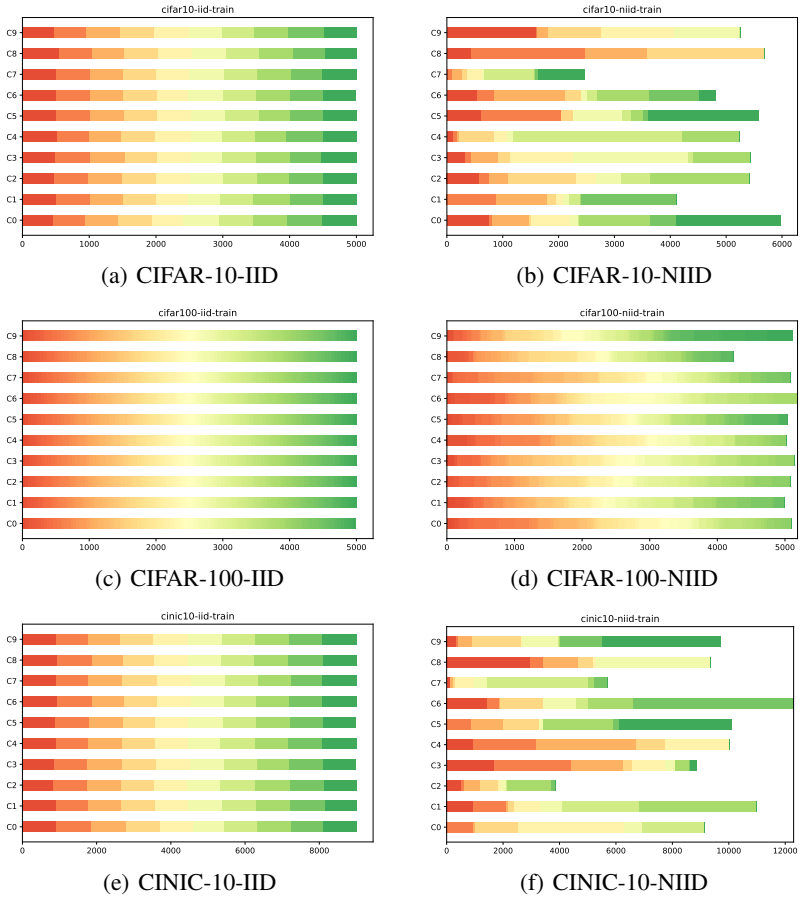
D Experimental Details

D.1 Datasets

To simulate federated learning scenario, we randomly split both the training and testing set of each dataset into K batches, and assign one training batch and one testing batch to each client. Namely, each client owns its local training set and testing set. We report the average accuracy on the local testing sets. For hyperparameter tuning, we take out a 15% subset of local training set for validation. After selecting the best hyperparameter, we return the validation set to the training set and retrain the model.

We are interested in two data partition strategies. 1) IID partition, where each client has a roughly equal proportion of each class. To create it, we randomly split samples in training or testing set into N balanced partitions and distribute one partition to each client. 2) NIID partition, where class proportions and number of data points of each client are unbalanced. Following [52, 30], we sample $p_i \sim Dir_K(0.5)$ and assign a $p_{i,k}$ proportion of the samples from class i to client k.

Because the image size of all the three adopted datasets is 32x32, the architecture of the feature extractor is not changed. The proposed *APFL* has three important hyperparameters, including the number of communication rounds, the number of selected clients per round, and the number of local epochs. In *FedCS*, for CIFAR-10, CIFAR-100 and CINIC-10, the super-network is trained for 600, 500, and 350 communication rounds respectively in the warm-up stage. As for full training with *FedAvg* or *FedPA*, we set the number of communication rounds as 2000, 1500, and 500 for CIFAR-10, CIFAR-100, and CINIC-10 respectively. The number of selected clients per round and that of local epochs are set to 10 and 1. In Figure 6, we visualize the class distributions among the training



(a) CIFAR-10-IID (b) CIFAR-10-NIID

(c) CIFAR-100-IID (d) CIFAR-100-NIID

(e) CINIC-10-IID (f) CINIC-10-NIID

Figure 6: Class distributions of the three datasets partitioned by IID and NIID strategy. Different colours represent samples from different classes.The horizontal axis represents the number of samples. The vertical axis stands for client ID.

sets of a population of non-identical or identical clients. As we can see, the class distributions of the IID versions are generally balanced, while those of the NIID versions are quite heterogeneous. Specifically, for NIID partition strategy, the number of samples varies for each client, and each client may have only a few categories of samples. Note that the class distribution of the testing set is the same as that of the training set, which means the local testing classes are the same as the local training classes. We divide all the samples of each dataset into 10 folds and assign one fold to a client. To make fair comparisons between different methods, the data distributions are fixed in our experiments.

D.2 Resource Constrained Setting

B_k have three possible configurations: high budget which requires that the FLOPs of the architecture is lower than 88M and the number of parameters is fewer than 2.2M; medium budget whose limit values for FLOPs and the number of parameters are 59M and 1.3M respectively; low budget whose limit values for FLOPs and the number of parameters are 28M and 0.7M respectively. The detailed settings are summarized in Table 2.

D.3 Model Architectures

We use MobileNetV2-1.5x as the Super-Network and set the shrink ratio in *FedCS* as 10%. There are two parts of our experiments involving a super-network. One is architecture search using *FedCS*. A super-network is first trained for a few communication rounds and then pruned locally on each client.

The other is using *FedPA* to train the sub-networks obtained by *FedCS* and *FedUniform*. A super-network is maintained on the server. For all of them, we use MobileNetV2-1.5x as the super-network and its details are listed in Table 3. In Table 4, 5, and 6, we also provide the details of the local architectures MobileNetV2-1x, MobileNetV2-0.75x and MobileNetV2-0.5x used in *FedUniform*. For CIFAR-100, we change the output dimension of linear layer to 100.

There are a total of 52 convolution layers in MobileNetV2-1.5x, but we only consider slimming 34 layers. The reason is that the output channel of a depthwise convolution [17] is always equal to that of its previous 1x1 convolution layer. Moreover, since we fix the input channel of the classifier, the output channel of the last convolution layer is also constant.

Table 2: Resource budgets of clients under different computation modes.

	High Budget Client	**Medium Budget Client**	**Low Budget Client**
Resource Constraints	FLOPs$\leq 88M$ Params$\leq 2.2M$	FLOPs$\leq 59M$ Params$\leq 1.3M$	FLOPs$\leq 28M$ Params$\leq 0.7M$
Proportion (HIGH CAPACITY)	50%	30%	20%
Proportion (LOW CAPACITY)	20%	30%	50%

Table 3: Detailed information of the Super-Network MobileNetV2-1.5x. For convolution layer (Conv2d), the parameters are listed with a sequence of input channel, output channel, kernel size, stride and padding. Note that the parameter "g" represents that the corresponding layer is a depth-wise convolution. For average pooling layer (AvgPool2d), we list the kernel size. For fully connected layer (Linear), we list the input dimension and the output dimension. There are skip connections in the bottlenecks where the input channels equals to the output channels and the stride of the first convolution layer equals 1.

Layer	**Details**	**Repetition**
	Conv2d(3, 48, k=(3, 3), s=(1, 1), pad=(1, 1))	$\times 1$
layer1	Conv2d(48, 48, k=(3, 3), s=(1, 1), pad=(1, 1), g=48) Conv2d(48, 24, k=(1, 1), s=(1, 1))	$\times 1$
layer2	Conv2d(24, 144, k=(1, 1), s=(1, 1)) Conv2d(144, 144, k=(3, 3), s=(1, 1), pad=(1, 1), g=144) Conv2d(144, 40, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(40, 240, k=(1, 1), s=(1, 1)) Conv2d(240, 240, k=(3, 3), s=(1, 1), pad=(1, 1), g=240) Conv2d(240, 40, k=(1, 1), s=(1, 1))	$\times 1$
layer3	Conv2d(40, 240, k=(1, 1), s=(1, 1)) Conv2d(240, 240, k=(3, 3), s=(2, 2), pad=(1, 1), g=240) Conv2d(240, 48, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(48, 288, k=(1, 1), s=(1, 1)) Conv2d(288, 288, k=(3, 3), s=(1, 1), pad=(1, 1), g=288) Conv2d(288, 48, k=(1, 1), s=(1, 1))	$\times 2$
layer4	Conv2d(48, 288, k=(1, 1), s=(1, 1)) Conv2d(288, 288, k=(3, 3), s=(2, 2), pad=(1, 1), g=288) Conv2d(288, 96, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(96, 576, k=(1, 1), s=(1, 1)) Conv2d(576, 576, k=(3, 3), s=(1, 1), pad=(1, 1), g=576) Conv2d(576, 96, k=(1, 1), s=(1, 1))	$\times 3$
layer5	Conv2d(96, 576, k=(1, 1), s=(1, 1)) Conv2d(576, 576, k=(3, 3), s=(1, 1), pad=(1, 1), g=576) Conv2d(576, 144, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(144, 864, k=(1, 1), s=(1, 1)) Conv2d(864, 864, k=(3, 3), s=(1, 1), pad=(1, 1), g=864) Conv2d(864, 144, k=(1, 1), s=(1, 1))	$\times 2$
layer6	Conv2d(144, 864, k=(1, 1), s=(1, 1)) Conv2d(864, 864, k=(3, 3), s=(2, 2), pad=(1, 1), g=864) Conv2d(864, 240, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(240, 1440, k=(1, 1), s=(1, 1)) Conv2d(1440, 1440, k=(3, 3), s=(1, 1), pad=(1, 1), g=1440) Conv2d(1440, 240, k=(1, 1), s=(1, 1))	$\times 2$
layer7	Conv2d(240, 1440, k=(1, 1), s=(1, 1)) Conv2d(1440, 1440, k=(3, 3), s=(1, 1), pad=(1, 1), g=1440) Conv2d(1440, 480, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(480, 1280, k=(1, 1), s=(1, 1))	$\times 1$
	AvgPool2d(k=(4, 4)) Linear(1280, 10)	$\times 1$ $\times 1$

Table 4: Detailed information of the Sub-Network MobileNetV2-1x used in *FedUniform*. For convolution layer (Conv2d), the parameters are listed with a sequence of input channel, output channel, kernel size, stride and padding. Note that the parameter "g" represents that the corresponding layer is a depthwise convolution. For average pooling layer (AvgPool2d), we list the kernel size. For fully connected layer (Linear), we list the input dimension and the output dimension. There are skip connections in the bottlenecks where the input channels equals to the output channels and the stride of the first convolution layer equals 1.

Layer	**Details**	**Repetition**
	Conv2d(3, 32, k=(3, 3), s=(1, 1), pad=(1, 1))	$\times 1$
layer1	Conv2d(32, 32, k=(3, 3), s=(1, 1), pad=(1, 1), g=48) Conv2d(32, 16, k=(1, 1), s=(1, 1))	$\times 1$
layer2	Conv2d(16, 96, k=(1, 1), s=(1, 1)) Conv2d(96, 96, k=(3, 3), s=(1, 1), pad=(1, 1), g=144) Conv2d(96, 24, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(24, 144, k=(1, 1), s=(1, 1)) Conv2d(144, 144, k=(3, 3), s=(1, 1), pad=(1, 1), g=240) Conv2d(144, 24, k=(1, 1), s=(1, 1))	$\times 1$
layer3	Conv2d(24, 144, k=(1, 1), s=(1, 1)) Conv2d(144, 144, k=(3, 3), s=(2, 2), pad=(1, 1), g=240) Conv2d(144, 32, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(32, 192, k=(1, 1), s=(1, 1)) Conv2d(192, 192, k=(3, 3), s=(1, 1), pad=(1, 1), g=288) Conv2d(192, 32, k=(1, 1), s=(1, 1))	$\times 2$
layer4	Conv2d(32, 192, k=(1, 1), s=(1, 1)) Conv2d(192, 192, k=(3, 3), s=(2, 2), pad=(1, 1), g=288) Conv2d(192, 64, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(64, 384, k=(1, 1), s=(1, 1)) Conv2d(384, 384, k=(3, 3), s=(1, 1), pad=(1, 1), g=576) Conv2d(384, 64, k=(1, 1), s=(1, 1))	$\times 3$
layer5	Conv2d(64, 384, k=(1, 1), s=(1, 1)) Conv2d(384, 384, k=(3, 3), s=(1, 1), pad=(1, 1), g=576) Conv2d(384, 96, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(96, 576, k=(1, 1), s=(1, 1)) Conv2d(576, 576, k=(3, 3), s=(1, 1), pad=(1, 1), g=864) Conv2d(576, 96, k=(1, 1), s=(1, 1))	$\times 2$
layer6	Conv2d(96, 576, k=(1, 1), s=(1, 1)) Conv2d(576, 576, k=(3, 3), s=(2, 2), pad=(1, 1), g=864) Conv2d(576, 160, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(160, 960, k=(1, 1), s=(1, 1)) Conv2d(960, 960, k=(3, 3), s=(1, 1), pad=(1, 1), g=1440) Conv2d(960, 160, k=(1, 1), s=(1, 1))	$\times 2$
layer7	Conv2d(160, 960, k=(1, 1), s=(1, 1)) Conv2d(960, 960, k=(3, 3), s=(1, 1), pad=(1, 1), g=1440) Conv2d(960, 320, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(320, 1280, k=(1, 1), s=(1, 1))	$\times 1$
	AvgPool2d(k=(4, 4)) Linear(1280, 10)	$\times 1$ $\times 1$

Table 5: Detailed information of the Sub-Network MobileNetV2-0.75x used in *FedUniform*. For convolution layer (Conv2d), the parameters are listed with a sequence of input channel, output channel, kernel size, stride and padding. Note that the parameter "g" represents that the corresponding layer is a depthwise convolution. For average pooling layer (AvgPool2d), we list the kernel size. For fully connected layer (Linear), we list the input dimension and the output dimension. There are skip connections in the bottlenecks where the input channels equals to the output channels and the stride of the first convolution layer equals 1.

Layer	**Details**	**Repetition**
	Conv2d(3, 24, k=(3, 3), s=(1, 1), pad=(1, 1))	$\times 1$
layer1	Conv2d(24, 24, k=(3, 3), s=(1, 1), pad=(1, 1), g=48) Conv2d(24, 16, k=(1, 1), s=(1, 1))	$\times 1$
layer2	Conv2d(16, 96, k=(1, 1), s=(1, 1)) Conv2d(96, 96, k=(3, 3), s=(1, 1), pad=(1, 1), g=144) Conv2d(96, 24, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(24, 144, k=(1, 1), s=(1, 1)) Conv2d(144, 144, k=(3, 3), s=(1, 1), pad=(1, 1), g=240) Conv2d(144, 24, k=(1, 1), s=(1, 1))	$\times 1$
layer3	Conv2d(24, 144, k=(1, 1), s=(1, 1)) Conv2d(144, 144, k=(3, 3), s=(2, 2), pad=(1, 1), g=240) Conv2d(144, 24, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(24, 144, k=(1, 1), s=(1, 1)) Conv2d(144, 144, k=(3, 3), s=(1, 1), pad=(1, 1), g=288) Conv2d(144, 24, k=(1, 1), s=(1, 1))	$\times 2$
layer4	Conv2d(24, 144, k=(1, 1), s=(1, 1)) Conv2d(144, 144, k=(3, 3), s=(2, 2), pad=(1, 1), g=288) Conv2d(144, 48, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(48, 288, k=(1, 1), s=(1, 1)) Conv2d(288, 288, k=(3, 3), s=(1, 1), pad=(1, 1), g=576) Conv2d(288, 48, k=(1, 1), s=(1, 1))	$\times 3$
layer5	Conv2d(48, 288, k=(1, 1), s=(1, 1)) Conv2d(288, 288, k=(3, 3), s=(1, 1), pad=(1, 1), g=576) Conv2d(288, 72, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(72, 432, k=(1, 1), s=(1, 1)) Conv2d(432, 432, k=(3, 3), s=(1, 1), pad=(1, 1), g=864) Conv2d(432, 72, k=(1, 1), s=(1, 1))	$\times 2$
layer6	Conv2d(72, 432, k=(1, 1), s=(1, 1)) Conv2d(432, 432, k=(3, 3), s=(2, 2), pad=(1, 1), g=864) Conv2d(432, 120, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(120, 720, k=(1, 1), s=(1, 1)) Conv2d(720, 720, k=(3, 3), s=(1, 1), pad=(1, 1), g=1440) Conv2d(720, 120, k=(1, 1), s=(1, 1))	$\times 2$
layer7	Conv2d(120, 720, k=(1, 1), s=(1, 1)) Conv2d(720, 720, k=(3, 3), s=(1, 1), pad=(1, 1), g=1440) Conv2d(720, 240, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(240, 1280, k=(1, 1), s=(1, 1))	$\times 1$
	AvgPool2d(k=(4, 4)) Linear(1280, 10)	$\times 1$ $\times 1$

Table 6: Detailed information of the Sub-Network MobileNetV2-0.5x used in *FedAvg* and *FedUniform*.For convolution layer (Conv2d), the parameters are listed with a sequence of input channel, output channel, kernel size, stride and padding. Note that the parameter "g" represents that the corresponding layer is a depthwise convolution. For average pooling layer (AvgPool2d), we list the kernel size. For fully connected layer (Linear), we list the input dimension and the output dimension. There are skip connections in the bottlenecks where the input channels equals to the output channels and the stride of the first convolution layer equals 1.

Layer	**Details**	**Repetition**
	Conv2d(3, 16, k=(3, 3), s=(1, 1), pad=(1, 1))	$\times 1$
layer1	Conv2d(16, 16, k=(3, 3), s=(1, 1), pad=(1, 1), g=48) Conv2d(16, 8, k=(1, 1), s=(1, 1))	$\times 1$
layer2	Conv2d(8, 48, k=(1, 1), s=(1, 1)) Conv2d(48, 48, k=(3, 3), s=(1, 1), pad=(1, 1), g=144) Conv2d(48, 16, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(16, 96, k=(1, 1), s=(1, 1)) Conv2d(96, 96, k=(3, 3), s=(1, 1), pad=(1, 1), g=240) Conv2d(96, 16, k=(1, 1), s=(1, 1))	$\times 1$
layer3	Conv2d(16, 96, k=(1, 1), s=(1, 1)) Conv2d(96, 96, k=(3, 3), s=(2, 2), pad=(1, 1), g=240) Conv2d(96, 16, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(16, 96, k=(1, 1), s=(1, 1)) Conv2d(96, 96, k=(3, 3), s=(1, 1), pad=(1, 1), g=288) Conv2d(96, 16, k=(1, 1), s=(1, 1))	$\times 2$
layer4	Conv2d(16, 96, k=(1, 1), s=(1, 1)) Conv2d(96, 96, k=(3, 3), s=(2, 2), pad=(1, 1), g=288) Conv2d(96, 32, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(32, 192, k=(1, 1), s=(1, 1)) Conv2d(192, 192, k=(3, 3), s=(1, 1), pad=(1, 1), g=576) Conv2d(192, 32, k=(1, 1), s=(1, 1))	$\times 3$
layer5	Conv2d(32, 192, k=(1, 1), s=(1, 1)) Conv2d(192, 192, k=(3, 3), s=(1, 1), pad=(1, 1), g=576) Conv2d(192, 48, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(48, 288, k=(1, 1), s=(1, 1)) Conv2d(288, 288, k=(3, 3), s=(1, 1), pad=(1, 1), g=864) Conv2d(288, 48, k=(1, 1), s=(1, 1))	$\times 2$
layer6	Conv2d(48, 288, k=(1, 1), s=(1, 1)) Conv2d(288, 288, k=(3, 3), s=(2, 2), pad=(1, 1), g=864) Conv2d(288, 80, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(80, 480, k=(1, 1), s=(1, 1)) Conv2d(480, 480, k=(3, 3), s=(1, 1), pad=(1, 1), g=1440) Conv2d(480, 80, k=(1, 1), s=(1, 1))	$\times 2$
layer7	Conv2d(80, 480, k=(1, 1), s=(1, 1)) Conv2d(480, 480, k=(3, 3), s=(1, 1), pad=(1, 1), g=1440) Conv2d(480, 160, k=(1, 1), s=(1, 1))	$\times 1$
	Conv2d(160, 1280, k=(1, 1), s=(1, 1))	$\times 1$
	AvgPool2d(k=(4, 4)) Linear(1280, 10)	$\times 1$ $\times 1$